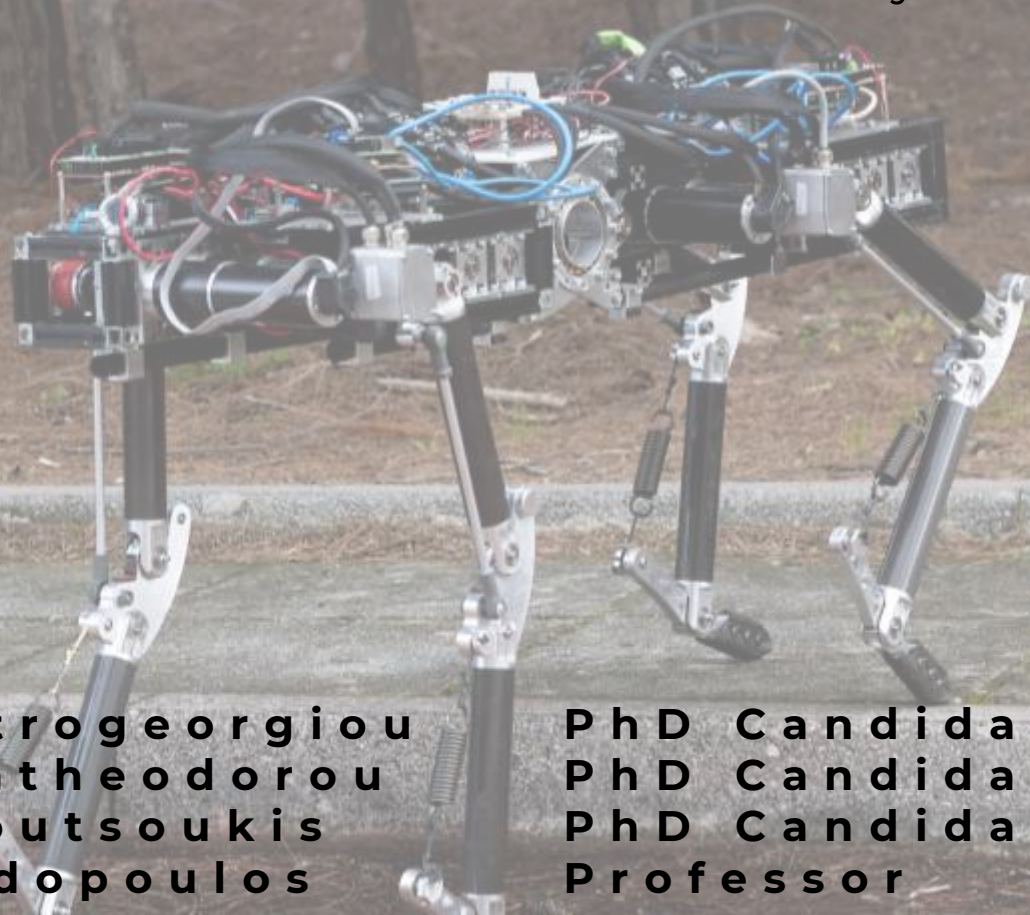


Learning Energy Efficient Trotting For Legged Robots

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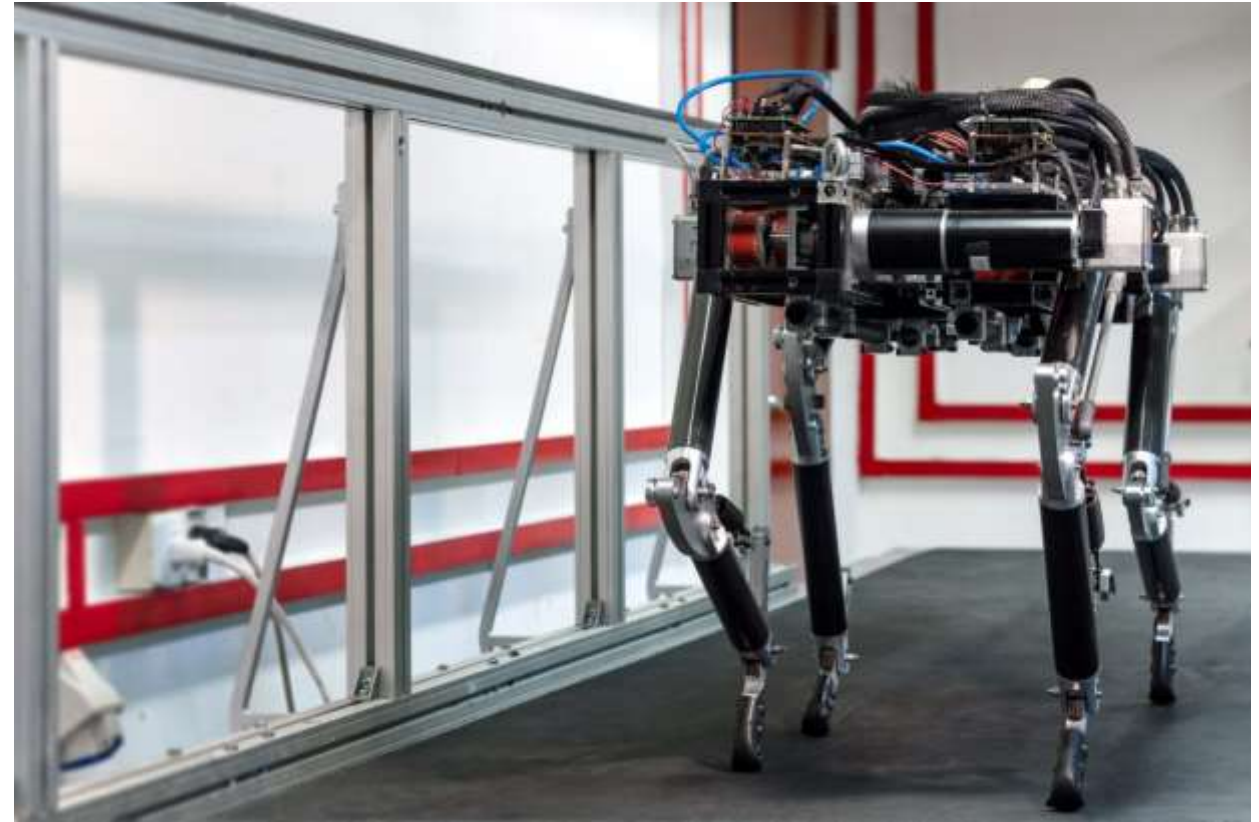
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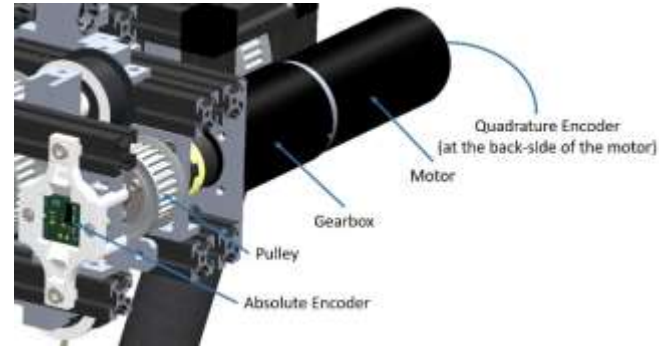
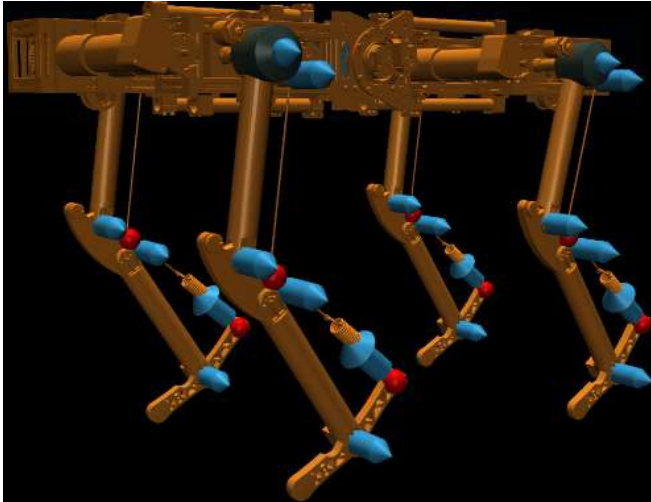
Overview



1. Laelaps II in MuJoCo
2. Laelaps II Toe Trajectory Planner
3. Training Framework
 - Reward Function
 - Observations & Actions
4. Results
5. Conclusions & Steps Forward



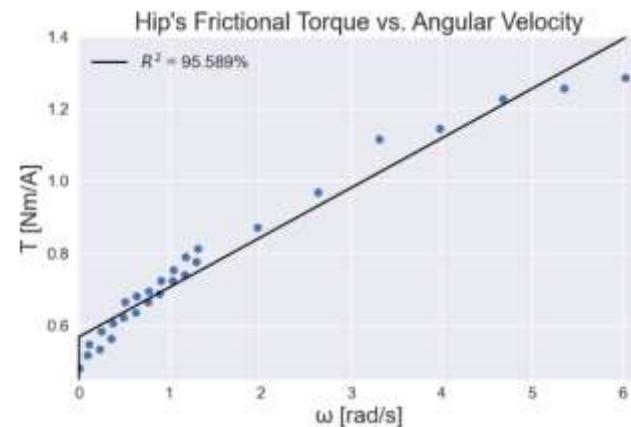
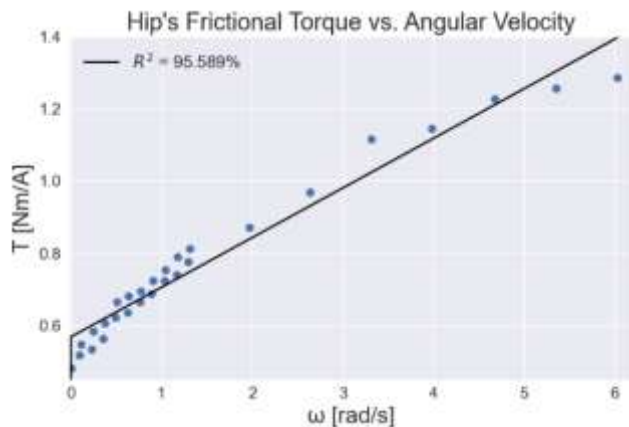
Laelaps II in MuJoCo



All the **electrical and mechanical properties** of the model were derived from the components' datasheets and/or were experimentally **verified**.

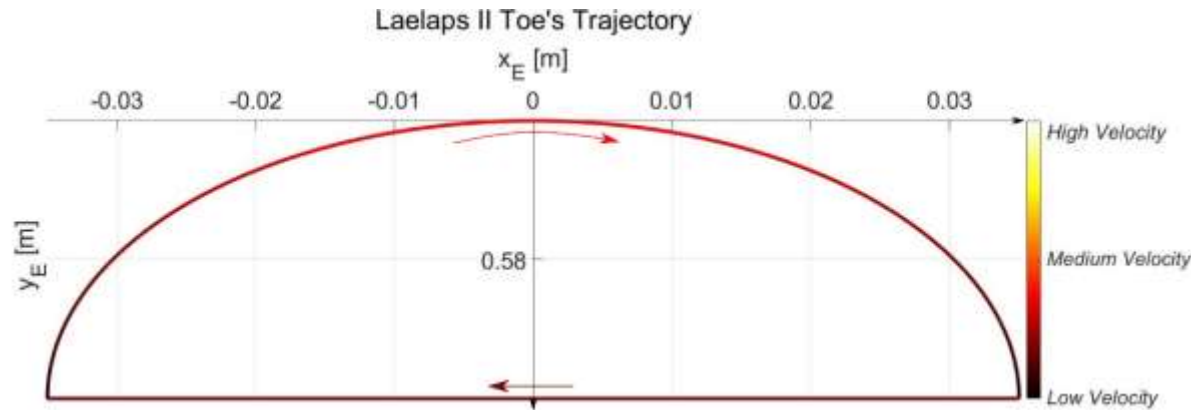
M u J o C o

- Created a **high-fidelity simulation**
- **Identified the frictional parameters** of each actuation unit, since they are directly connected to energy consumption



$$\tau_i = f_1 \dot{q}_i + f_2 \text{sign}(\dot{q}_i)$$

Toe Trajectory Planner



Swing Phase $t_{leg} < T_{swing}$

$$x_{toe,leg}(t_{leg}) = x_{c,leg} + a_{leg} \cos(\theta_{traj} + dir_{leg} \cdot \pi), \text{ with } \theta_{traj} = \frac{\pi}{2} (\cos(\pi t_{leg} / T_{swing}) + 1)$$

$$y_{toe,leg}(t_{leg}) = y_{c,leg} + b_{leg} \sin(\theta_{traj})$$

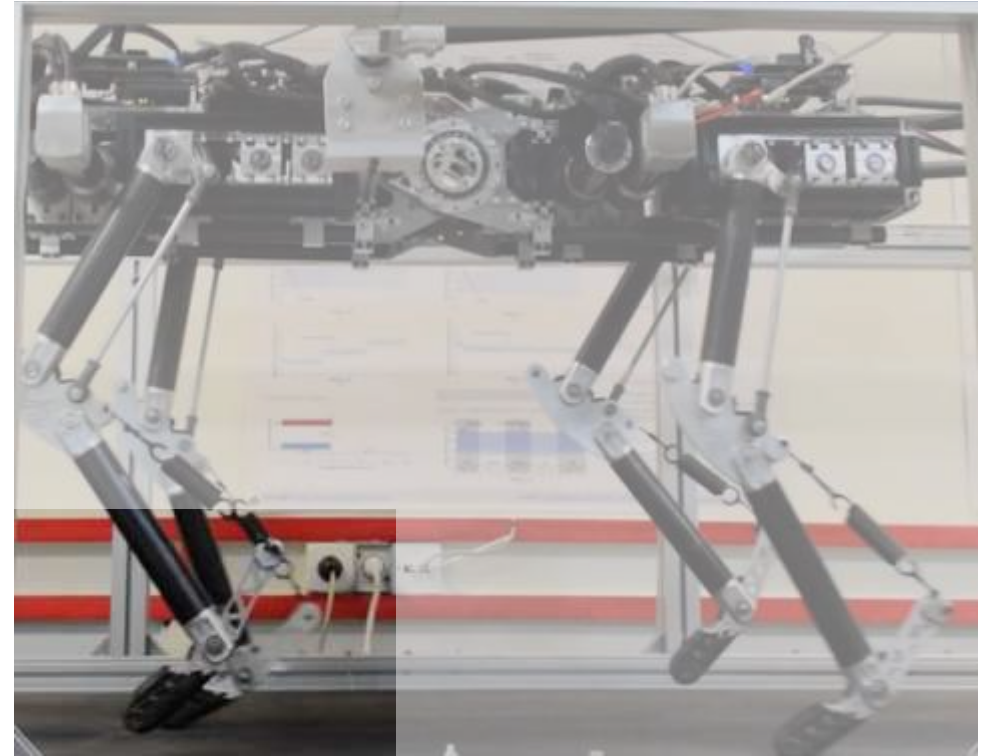
Stance Phase $t_{leg} \geq T_{swing}$

$$x_{toe,leg}(t_{leg}) = x_{c,leg} + (1 - 2 \cdot dir_{leg}) \cdot (a_{leg} - (t_{leg} - T_{swing}) \cdot V), \quad V = 2a_{leg} / T_{stance}$$

$$y_{toe,leg}(t_{leg}) = y_{c,leg}$$

$$t_{leg} = \text{mod}(t + dt_{phase}, T_{step}), \text{ with } T_{step} = T_{swing} + T_{stance}$$

$$dir_{leg} = \begin{cases} 0, & \text{Forward Motion} \\ 1, & \text{Backward Motion} \end{cases}$$



Reward Function



$$E_{act} = \int_{t_1}^{t_2} \sum_{i=1}^8 |\tau_{m,i} \dot{q}_{m,i}| dt$$

Mechanical power of
the actuators

&

$$E_{el} = \int_{t_1}^{t_2} \sum_{i=1}^8 \left[\left(\frac{\tau_{m,i}}{K_{T,i}} \right)^2 R_{m,i} \right] dt$$

Electric losses

$$rew_{en} = -w_{en} \frac{E_{tot}}{\Delta x_{ep} + \epsilon}$$

ϵ is introduced to
avoid division by ~ 0

+

$$rew_x = w_x (|x_{now} - x_{previous}|) \quad \& \quad rew_y = -w_y (|y_{now}| - |y_{previous}|)$$

=

$$rew_{tot} = rew_x + rew_y + rew_{en}$$

Actions & Observations

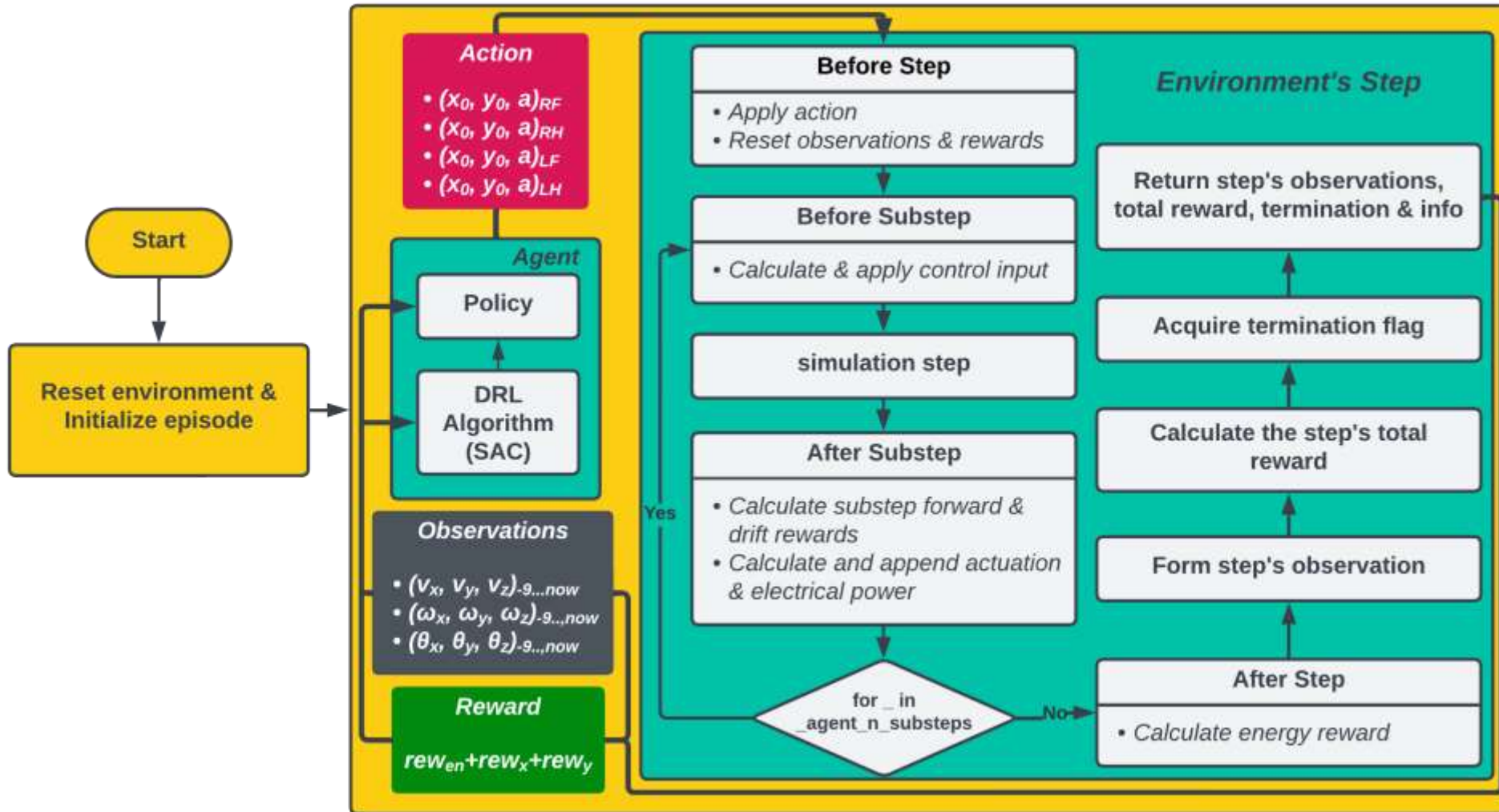
$$\left[\left(x_0, y_0, a \right)_{RF}, \left(x_0, y_0, a \right)_{RH}, \left(x_0, y_0, a \right)_{LF}, \left(x_0, y_0, a \right)_{LH} \right] \in \mathbb{R}^{12 \times 1}$$

- The **action space** consists of the **coordinates of the center** & the **a radius of the semi elliptical trajectory** (for each toe, i.e.: RF, RH, LF, LH)
- The **horizontal radius (a)** is directly coupled to the body's **velocity** & **direction** and thus to its **kinetic energy**

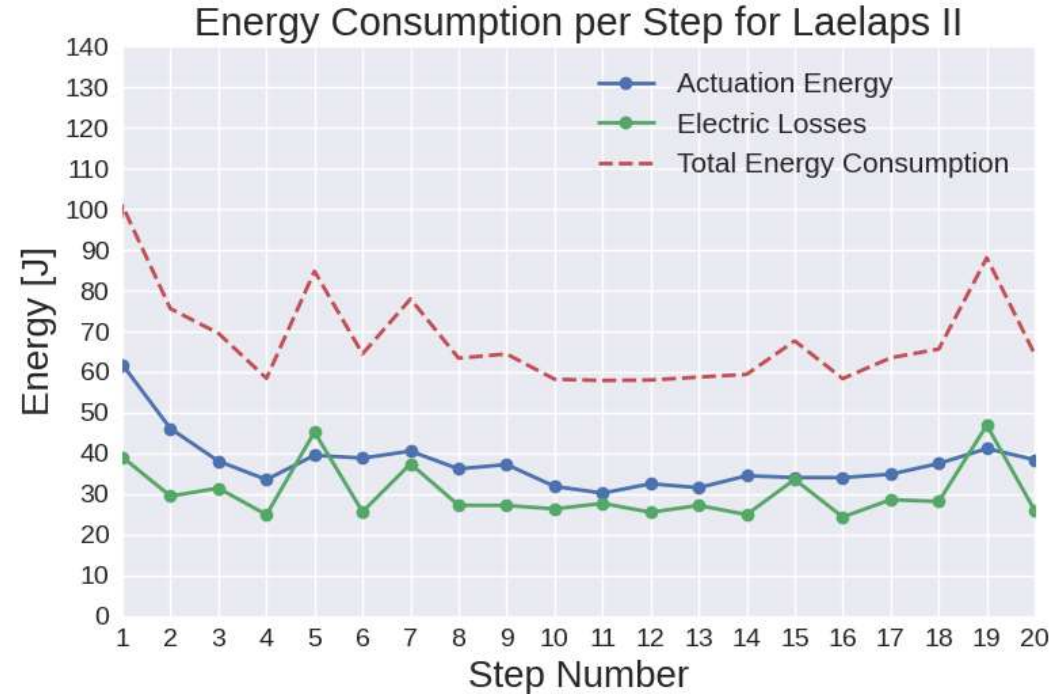
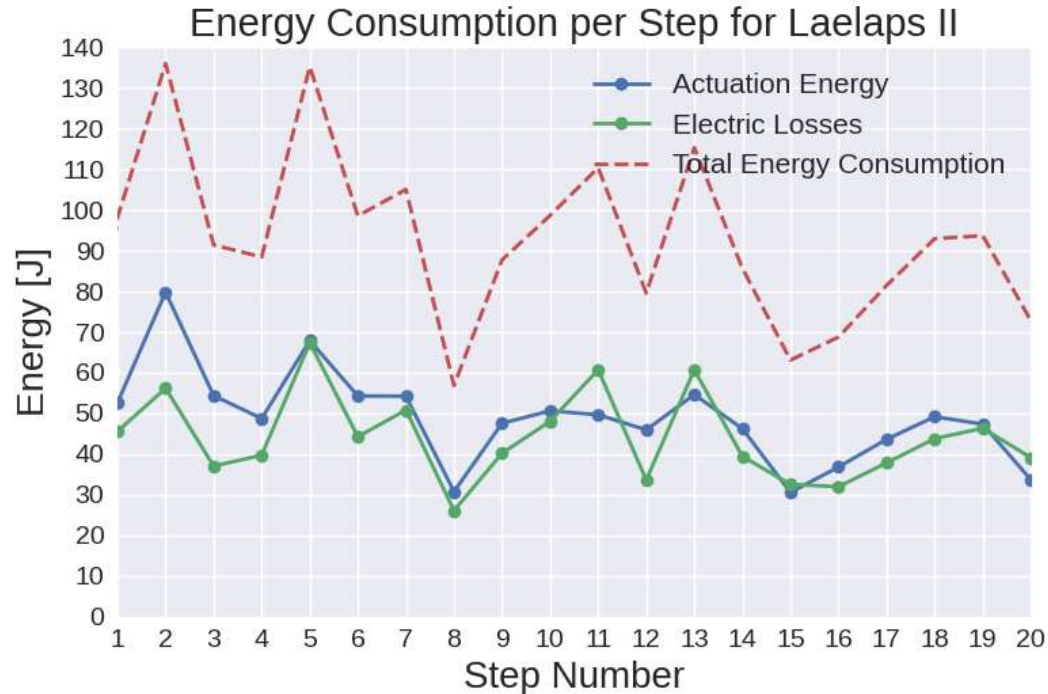
$$\left[\left(v_x, v_y, v_z \right)_{t-9\dots now}, \left(\omega_x, \omega_y, \omega_z \right)_{t-9\dots now}, \left(\theta_x, \theta_y, \theta_z \right)_{t-9\dots now} \right] \in \mathbb{R}^{90 \times 1}$$

- The **observation space** consists of the **linear and angular components of the body's velocity** along with its **roll-pitch-yaw angles**
- The **observations time progress** is also included in the observation space

Training Framework



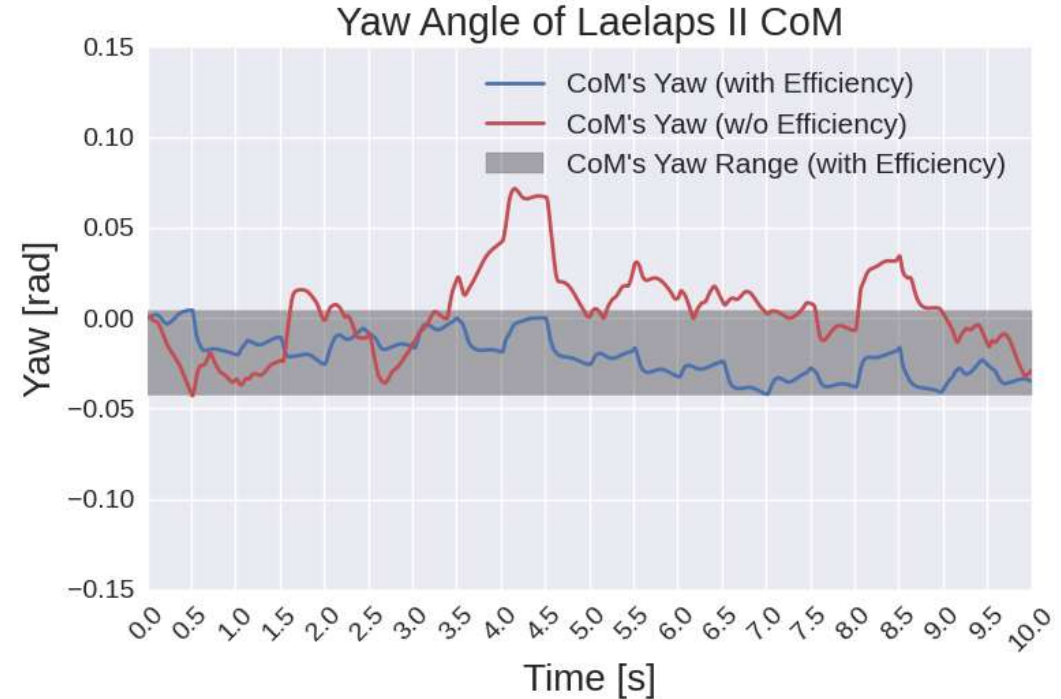
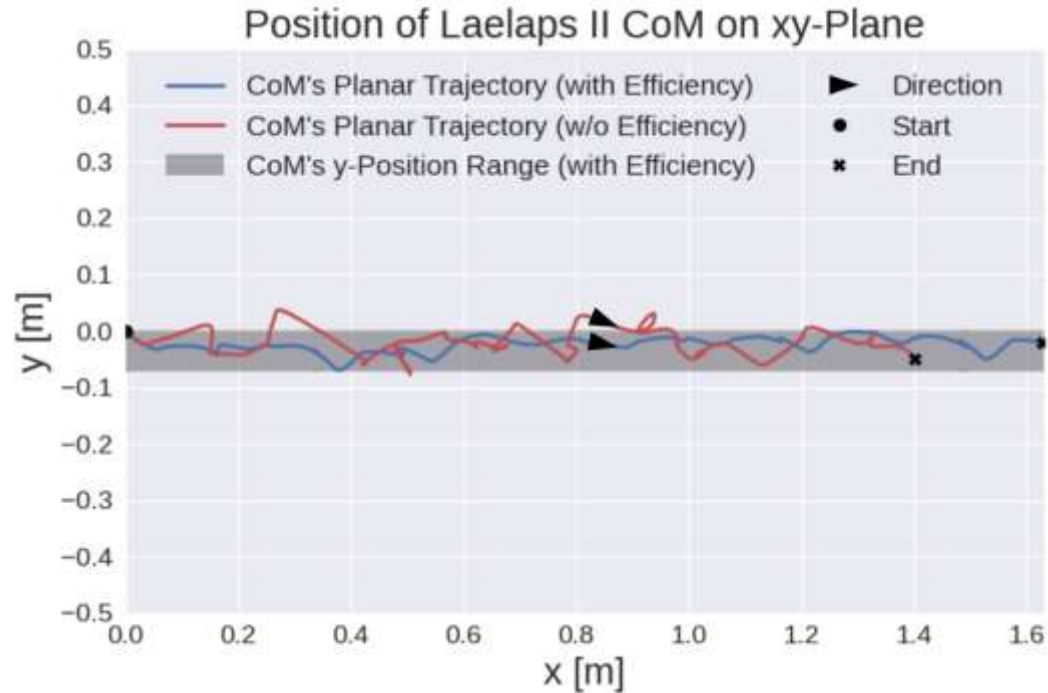
Results 1/3 – Energy Consumption



- By penalizing electrical losses and the mechanical power, total energy consumption of Laelaps II is significantly reduced

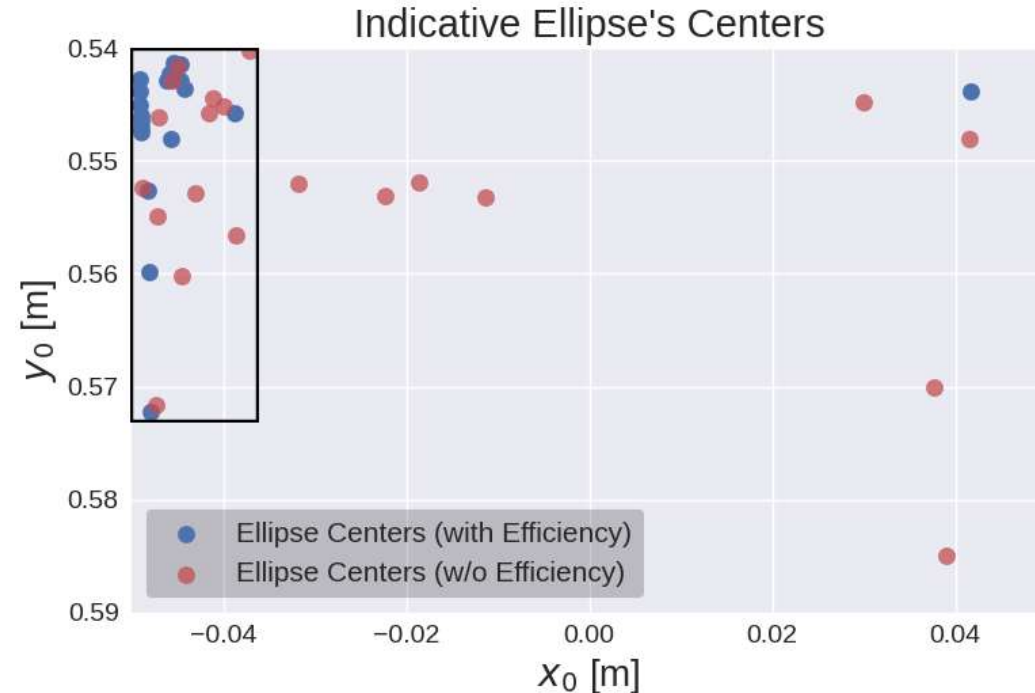
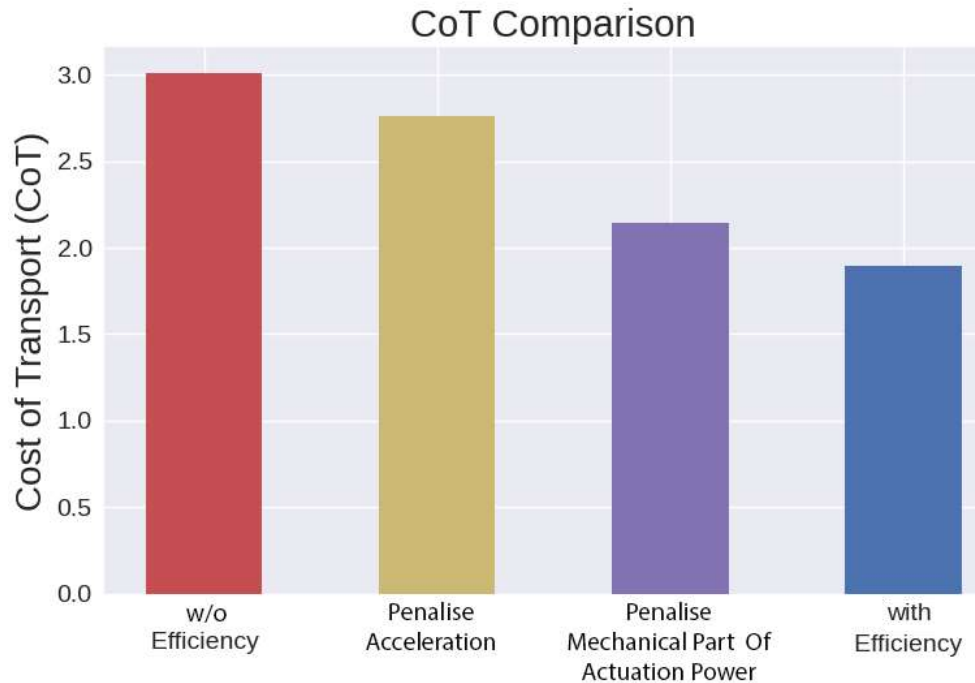
$$rew_{en} = -w_{en} \frac{E_{tot}}{\Delta x_{ep} + \epsilon}$$

Results 2/3 – Motion Quality



- Applying the energy efficient term in the training framework produces smoother motions, i.e.:
 - Bounded body yaw angles, i.e.: the quadruped is not diverging from its desired straight-line motion
 - Longer distance covered

Results 3/3 – CoT & Footsteps



- Compared to similar learning approaches the **proposed reward function** produces motions with **lower CoT**
- The **produced footsteps** tend to be within a specific area of the leg's workspace.

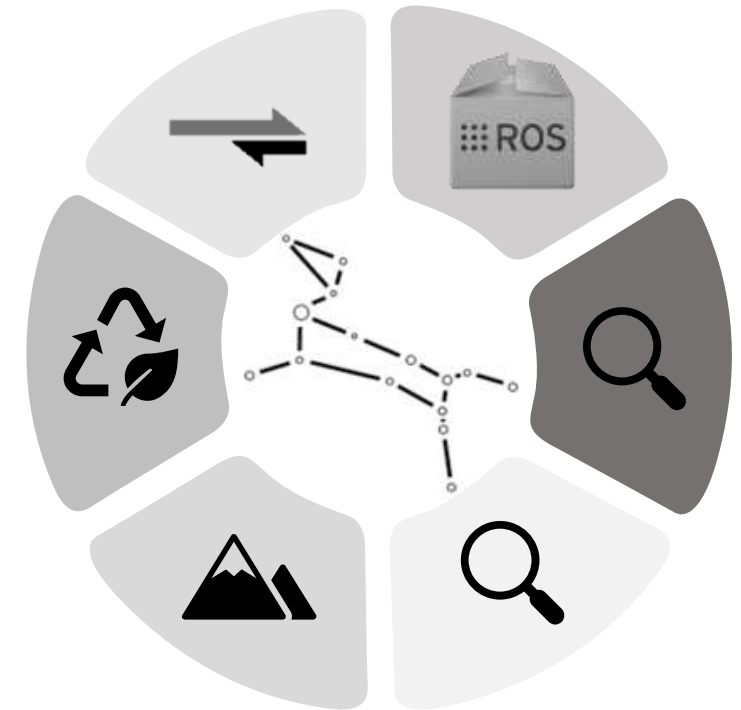
Conclusion



1. Smoother produced motions
2. Reduced CoT by 37%
3. Smaller ranges in body angles – fewer corrective actions were needed during the transition to the goal
4. The footsteps, i.e., ellipse centers and a radii, produced by the proposed DRL control scheme tended to be within a specific area of the leg's workspace
5. Previous analytical studies reached similar conclusions

Next Steps

- Apply the learned policies to *Laelaps II* on the treadmill utilizing our *ether_ros2* ROS2 package
- Investigate how the gains of the low-level PV controllers affect energy efficiency and include them in the DRL action space
- Investigate how the observations space could be expanded with terms that improve the quality & the efficiency of the robot's motion
- Adapt the current framework to produce energy efficient motion on rough terrain
- Validate analytical approaches on energy efficiency using DRL



Indicative References



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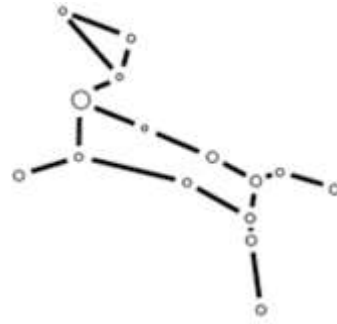
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THANK YOU



check our work @
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